FORMULAS FOR SEQUENCES AND SER IES

|  | DESCRIPTION OF FORMULA | FORMULA |
| :---: | :---: | :---: |
|  | Recursive Formula Arithmetic Sequence | $a_{n}=a_{(n-1)}+d$ <br> Where dis the commondifference. |
|  | Recursive Formula Geometric Sequence | $a_{n}=r \cdot a_{(n-1)}$ <br> Where is the common ratio. |
|  | $n$th term of an Arithmetic Sequence | $a_{n}=a_{1}+(n-1) d$ <br> Where $n$ is any natural number. |
|  | GENERAL <br> Sum of an Arithmetic Series | $S_{n}=n\left[\frac{a_{1}+a_{n}}{2}\right]$ |
|  | ALTERNATE <br> Sum of an Arithmetic Series | $S_{n}=\frac{n}{2}\left[2 a_{1}+(n-1) d\right]$ |
|  | Sigma Notation <br> Sum of an Arithmetic Series | $\sum_{k=1}^{n} f(k)$ <br> Where $k=1$ is the first value of $k, n$ is the last value $k$, and $f(k)$ is the formula for the terms of the series. |
|  | $n$th term of a Geometric Sequence | $a_{n}=a_{1} \cdot r^{(n-1)}$ <br> Where $n$ is any natural number. |
|  | Sum of a Geometric Series (Use when given $a_{1}$ and $n$.) | $S_{n}=\frac{a_{1}-a_{1} r^{n}}{1-r}, \text { and } r \neq 1$ |
|  | Sum of a Geometric Series (Use when given $a_{1}$ and $\mathrm{a}_{n}$.) | $S_{n}=\frac{a_{1}-a_{n} r}{1-r}, \text { and } r \neq 1$ |
|  | Sum of a Geometric Series (Use when given $a_{1}$ and $\mathrm{a}_{\mathrm{n}}$.) | $S_{n}=\frac{a_{1}\left(1-r^{n}\right)}{1-r} \text {, and } r \neq 1$ |
|  | Sigma Notation <br> Sum of a Geometric Series | $\sum_{k=1}^{n} a_{1}(b)^{(k-1)}$ <br> Where $k$ is the first value of $k, n$ is the last value of $k$, $a_{1}$ is the first term, and $b$ is the base. |
|  | Sum of an Infinite Geometric Series | $\begin{aligned} & S=\frac{a_{1}}{1-r} \text {, with }-1<r<1 \\ & \text { If }\|r\| \geq 1 \text {, the series has no sum. } \end{aligned}$ |
|  | Sigma Notation <br> Sum of an Infinite Geometric Series | $\sum_{k=1}^{\infty} a_{1}(b)^{(k-1)}$ <br> Where $k$ is the first value of $k$, the last value of $k$ is infinite, $a_{1}$ is the first term, and $b$ is the base. |
|  | Binomial Theorem $(a+b)^{n}=$${ }_{n} C_{0} a^{n} b^{0}+{ }_{n} C_{1} a^{(n-1)} b^{1}+{ }_{n} C_{2} a^{(n-2)} b^{2}+{ }_{n} C_{3} a^{(n-3)} b^{3}+\ldots+{ }_{n} C_{n} a^{0} b^{n}=\sum_{k=0}^{n} \frac{n!!(n-k)!}{k!} \cdot a^{n-k} b^{k}$ |  |

