

Algebra

absolute value $ x $	$ x = \begin{cases} x, & \text{if } x \geq 0 \\ -x, & \text{if } x < 0 \end{cases}$
absolute value $ x - y $	the distance between 2 points, x and y , on a number line
distance formula	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ = distance between 2 points (x_1, y_1) and (x_2, y_2) on coordinate plane
midpoint formula	$M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$ = (average x coordinates., average y coordinates)
slope of a line between any 2 points (x_1, y_1) and (x_2, y_2)	$m = \frac{y_2 - y_1}{x_2 - x_1}$ slope is the measure of the steepness of a line horizontal line slope = 0; vertical line slope is undefined parallel lines have equal slopes; perpendicular lines - slopes are opposite (negative) reciprocals; product of slopes = -1
linear equation slope intercept form point-slope form standard form	$y = mx + b$, where m = slope and b = y coordinate of the y-intercept $y - y_1 = m(x - x_1)$ $Ax + By = C$
equations for a circle	$x^2 + y^2 = r^2$ circle centered at $(0, 0)$ with radius r $(x - h)^2 + (y - k)^2 = r^2$ circle centered at (h, k) with radius r
equations for parabola	$y = a(x - h)^2 + k$ parabola opens up or down; vertex at (h, k) $x = a(y - k)^2 + h$ parabola opens left or right; vertex at (h, k)
factoring difference of 2 squares sum of 2 squares difference of 2 cubes sum of 2 cubes perfect square trinomials	$a^2 - b^2 = (a + b)(a - b)$ prime (not factorable) $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$ $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ $(a + b)^2 = a^2 + 2ab + b^2$ and $(a - b)^2 = a^2 - 2ab + b^2$
quadratic formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ yields solutions for $ax^2 + bx + c = 0$ Note: the sum of the two solutions is $-\frac{b}{a}$ and product of solutions = $\frac{c}{a}$
discriminant test	$b^2 - 4ac = 0 \rightarrow$ one real solution $b^2 - 4ac > 0 \rightarrow$ two real solutions $b^2 - 4ac < 0 \rightarrow$ two complex conjugate solutions
exponent rules	$x^0 = 1$ $(x^a)^b = x^{ab}$ $x^a x^b = x^{a+b}$ $\frac{x^a}{x^b} = x^{a-b}$ $x^{-a} = \frac{1}{x^a}$ and $\frac{1}{x^{-a}} = x^a$
radicals and exponents	$\sqrt{x} = x^{1/2}$ $\sqrt[3]{x} = x^{1/3}$ $\sqrt[b]{x^a} = x^{a/b}$
complex number	$i = \sqrt{-1}$ $i^2 = -1$ $i^3 = -i$ $i^4 = 1$
absolute value equation	If algebraic expression = A , then set up two equations and solve: algebraic expression = A and algebraic expression = -A
absolute value inequalities	If algebraic expression < A , then set up compound inequality (conjunction) and solve: -A < algebraic expression < A If algebraic expression > A , then set up two inequalities (disjunction) and solve: algebraic expression > A or algebraic expression < -A

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1 1
1 2 1
1 3 3 1
1 4 6 4 1
1 5 10 10 5 1

Algebra

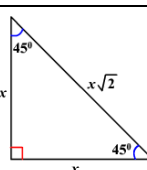
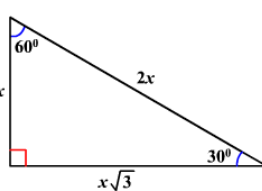
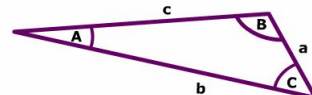
distance	$d = rt$ distance = rate x time
average (mean)	$average = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n}$
% change	$percent\ change = \frac{change\ in\ quantity}{original\ quantity}$
proportion	$\frac{a}{b} = \frac{c}{d}$ implies $ad = bc$ by cross-multiplication
direct variation	$y = kx$ or $\frac{x_1}{y_1} = \frac{x_2}{y_2}$ where k is the constant of variation
inverse variation	$xy = k$ or $x_1y_1 = x_2y_2$ where k is the constant of variation
arithmetic sequence	$a_n = a_1 + (n-1)d$, n th term of arithmetic sequence, d is the common difference between terms
arithmetic series	$S_n = \frac{n(a_1 + a_n)}{2}$, S_n = sum of first “n” terms of a finite arithmetic series; a_1 = first term
geometric sequence	$a_n = a_1r^{n-1}$ n th term of the geometric series; r is the common ratio
geometric series	$S_n = a_1 + a_1r + \dots + a_1r^{n-1} = \frac{a_1(1-r^n)}{1-r}$, S_n = sum of first “n” terms of geometric series
combinations	${}_nC_r = \frac{n!}{r!(n-r)!}$ number of combinations of n items taken r at a time; order does not matter;
permutations	${}_nP_r = \frac{n!}{(n-r)!}$ number of ways to arrange n items taken r at a time; order does matter;
degrees to radian measure	multiply angle in degrees by $\frac{\pi}{180^\circ}$
logarithms	$\log_b y = x$ means $y = b^x$ $\log_b MN = \log_b M + \log_b N$ $\log_b \left(\frac{M}{N}\right) = \log_b M - \log_b N$ $\log_b M^N = N \log_b M$ $\log_b M = \frac{\log_c M}{\log_c b}$ (change of base formula)

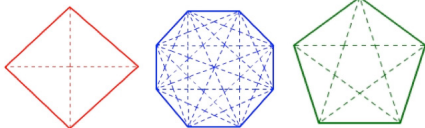
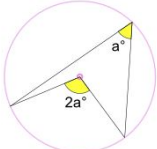
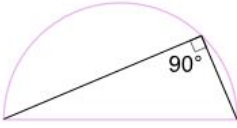
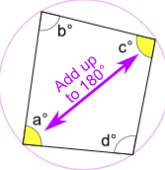
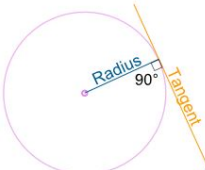
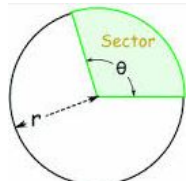
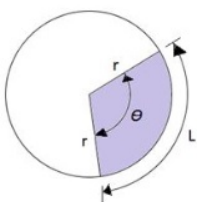
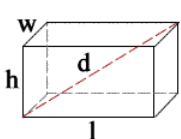
Geometry

Perimeter	In general, perimeter = sum of lengths of sides
square	$P = 4s$
rectangle	$P = 2L + 2W$
circle	$C = 2\pi r$ (circumference)

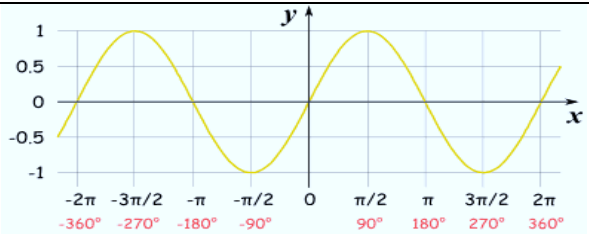
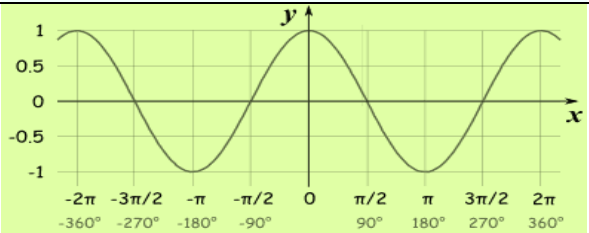
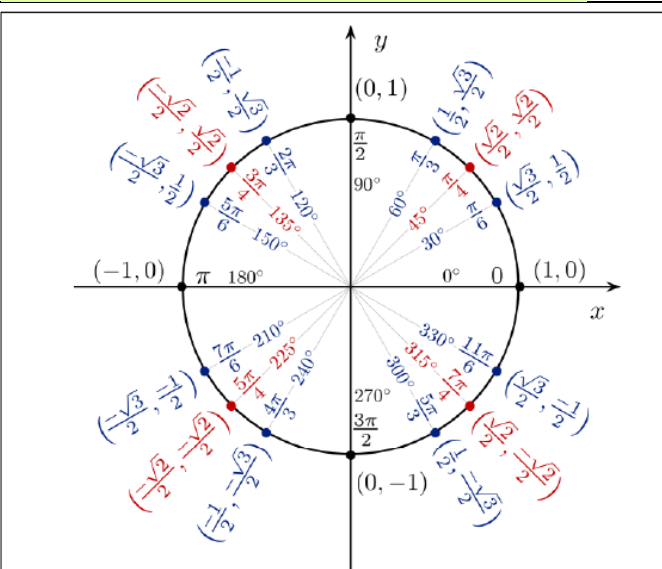
Area	Note that the units are square units.
square	$A = s^2$
rectangle, parallelogram	$A = bh$ (note base and height are <i>always</i> perpendicular)
triangle	$A = \frac{1}{2}bh$
circle	$A = \pi r^2$
trapezoid	$A = \frac{1}{2}(b_1 + b_2)h$ (average of bases times the height)

Volume	B = area of base; h = height
cube	$V = Bh = s^3$ where s is the side length
rectangular prism	$V = Bh = lwh$
sphere	$V = \frac{4}{3}\pi r^3$
cone	$V = \frac{1}{3}\pi r^2h$
cylinder	$V = Bh = \pi r^2h$

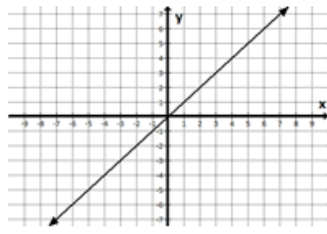
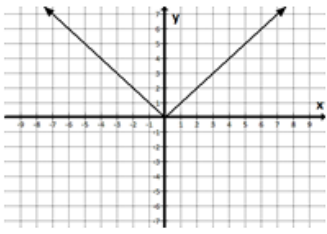
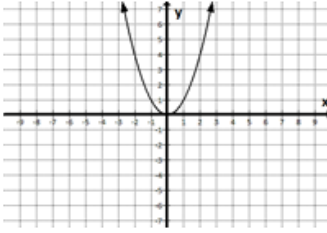
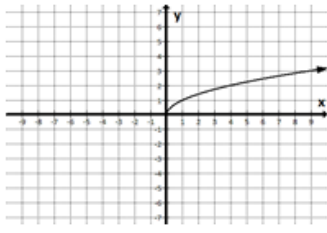
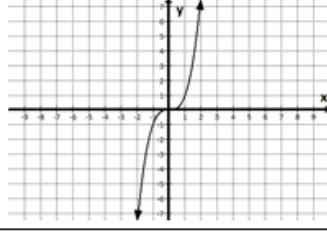
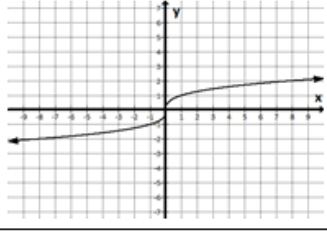
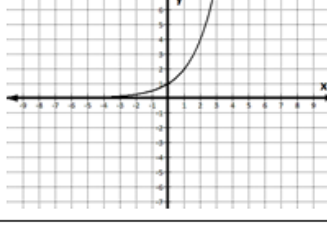
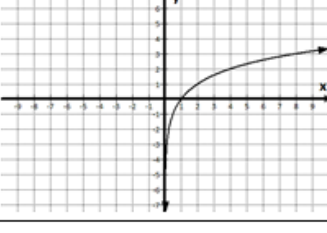
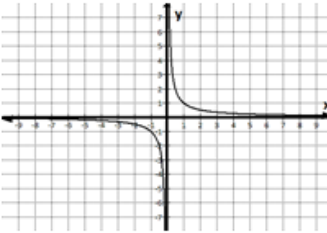
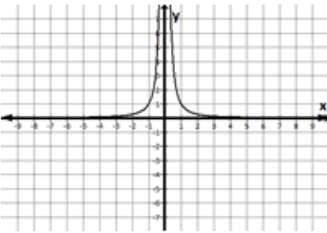
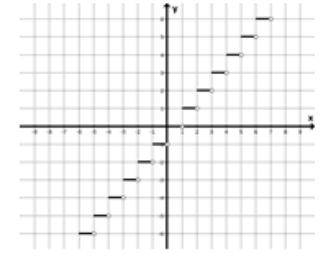
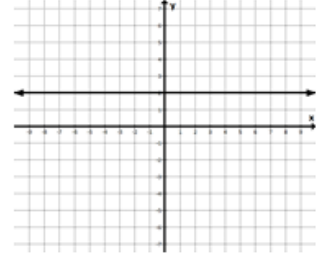
Triangles									
Congruency Theorems	SSS, SAS, ASA, or AAS or use H-L (right triangles only)								
Pythagorean Theorem	$c^2 = a^2 + b^2$ is used to find length of sides or hypotenuse, c , for a right triangle If $c^2 = a^2 + b^2$, then the triangle is a right triangle (Converse of Pythagorean Theorem) If $c^2 < a^2 + b^2$, then the triangle is acute If $c^2 > a^2 + b^2$, then the triangle is obtuse								
Common Pythagorean Triples	<table style="display: inline-table; border: none;"> <tr> <td>3 - 4 - 5</td> <td>5 - 12 - 13</td> <td>7 - 24 - 25</td> <td>8 - 15 - 17</td> </tr> <tr> <td>6 - 8 - 10</td> <td>10 - 24 - 26</td> <td>14 - 48 - 50</td> <td>16 - 30 - 34</td> </tr> </table>	3 - 4 - 5	5 - 12 - 13	7 - 24 - 25	8 - 15 - 17	6 - 8 - 10	10 - 24 - 26	14 - 48 - 50	16 - 30 - 34
3 - 4 - 5	5 - 12 - 13	7 - 24 - 25	8 - 15 - 17						
6 - 8 - 10	10 - 24 - 26	14 - 48 - 50	16 - 30 - 34						
45-45-90 triangle	ratios of sides lengths: $1x : 1x : x\sqrt{2}$ 								
30-60-90 triangle	ratios of sides lengths: $1x : x\sqrt{3} : 2x$ 								
Law of Sines and Law of Cosines (for non-right triangles)	For non -right triangles, use the Law of Sines to find side lengths and angles when possible, or use Law of Cosines when you have 2 sides and the included angle .  $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$ $c^2 = a^2 + b^2 - 2bc \cos C$								

Other Formulas and Facts	
sum of interior angles of a convex polygon	$S = (n - 2)180^\circ$, $n = \#$ of sides
sum of exterior angles in a convex polygon	sum of exterior angles always equals 360°
number of diagonals in a convex polygon	<p>Example:</p>  <p># of diagonals = $\frac{n(n-3)}{2}$, where n = number of sides</p>
inscribed angle facts	  <p>An inscribed angle a is half the central angle, $2a$. Therefore, the inscribed angle 90° is half of the central angle 180°.</p>  <p>A Cyclic Quadrilateral's opposite angles add up to 180°: $a + c = 180^\circ$ $b + d = 180^\circ$</p>  <p>A tangent is a line that just touches a circle at one point. It always forms a right angle with the circle's radius to the point of tangency.</p>
sector area of a circle	 <p>$A = \frac{\theta^\circ}{360^\circ} \cdot \pi r^2 =$ fractional part of the circle's area</p>
length of intercepted arc	 <p>$L = \frac{\theta^\circ}{360^\circ} \cdot 2\pi r =$ fractional part of the circumference</p>
Length of diagonal of a rectangular prism	 <p>$d = \sqrt{L^2 + H^2 + W^2}$</p>


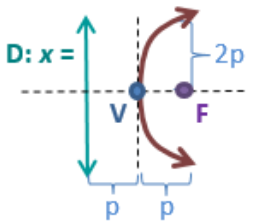
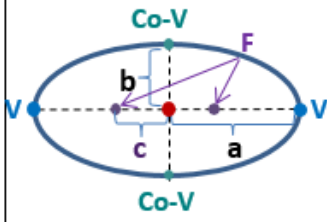
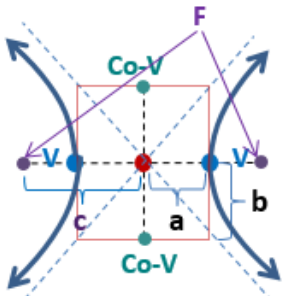
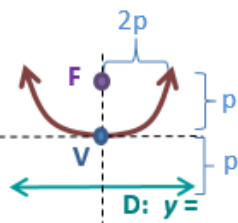
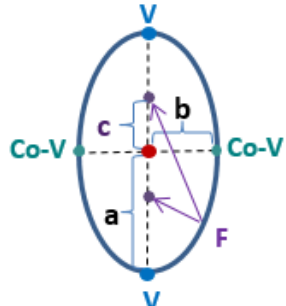
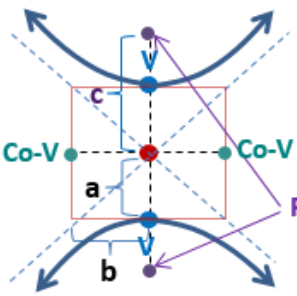
Trigonometry

Trigonometric ratios	$\sin \Theta = \frac{opp}{hyp} = \frac{y}{r}$ $\cos \Theta = \frac{adj}{hyp} = \frac{x}{r}$ $\tan \Theta = \frac{\sin \Theta}{\cos \Theta} = \frac{opp}{adj} = \frac{y}{x}$	$\csc \Theta = \frac{1}{\sin \Theta} = \frac{hyp}{opp} = \frac{r}{y}$ $\sec \Theta = \frac{1}{\cos \Theta} = \frac{hyp}{adj} = \frac{r}{x}$ $\cot \Theta = \frac{\cos \Theta}{\sin \Theta} = \frac{adj}{opp} = \frac{x}{y}$																			
Trig identities	$\sin^2 \Theta + \cos^2 \Theta = 1$	$1 + \cot^2 \Theta = \csc^2 \Theta$	$1 + \tan^2 \Theta = \sec^2 \Theta$																		
Law of Sines	$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$																				
Law of Cosines	$c^2 = a^2 + b^2 - 2ab \cos C$																				
Sine & Cosine functions	$y = A \sin(Bx + C) + D$ $y = A \cos(Bx + C) + D$	<i>Amplitude</i> = $ A $ <i>Horizontal shift</i> = $-\frac{C}{B}$	<i>Period</i> = $\frac{2\pi}{B}$ <i>Vertical shift</i> = D																		
Graph of $y = \sin x$	 <p>The graph shows a sine wave oscillating between y = 1 and y = -1. The x-axis is labeled with radians from -2π to 2π and degrees from -360° to 360°. Key points are marked at $(-\pi, 0)$, $(-\pi/2, -1)$, $(0, 0)$, $(\pi/2, 1)$, and $(\pi, 0)$.</p>																				
Graph of $y = \cos x$	 <p>The graph shows a cosine wave oscillating between y = 1 and y = -1. The x-axis is labeled with radians from -2π to 2π and degrees from -360° to 360°. Key points are marked at $(-2\pi, 1)$, $(-\pi, -1)$, $(0, 1)$, $(\pi, -1)$, and $(2\pi, 1)$.</p>																				
Unit Circle	$x = \cos \theta$ $y = \sin \theta$ $180^\circ = \pi \text{ radians}$		<table border="1"> <thead> <tr> <th>degrees</th> <th>radians</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td></tr> <tr><td>30</td><td>$\pi/6$</td></tr> <tr><td>45</td><td>$\pi/4$</td></tr> <tr><td>60</td><td>$\pi/3$</td></tr> <tr><td>90</td><td>$\pi/2$</td></tr> <tr><td>180</td><td>π</td></tr> <tr><td>270</td><td>$3\pi/2$</td></tr> <tr><td>360</td><td>2π</td></tr> </tbody> </table>	degrees	radians	0	0	30	$\pi/6$	45	$\pi/4$	60	$\pi/3$	90	$\pi/2$	180	π	270	$3\pi/2$	360	2π
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270	$3\pi/2$																				
360	2π																				
	 <p>The unit circle diagram shows angles from 0° to 360° in increments of 30°. The corresponding sine and cosine values are written at each angle. For example, at 30°, $\sin 30^\circ = 1/2$ and $\cos 30^\circ = \sqrt{3}/2$. The four quadrants are labeled with their respective signs for sine and cosine.</p>																				

Graphs

Parent Function	Graph	Parent Function	Graph
$y = x$ Linear, Odd Domain: $(-\infty, \infty)$ Range: $(-\infty, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow -\infty$ $x \rightarrow \infty, y \rightarrow \infty$		$y = x $ Absolute Value, Even Domain: $(-\infty, \infty)$ Range: $[0, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow \infty$ $x \rightarrow \infty, y \rightarrow \infty$	
$y = x^2$ Quadratic, Even Domain: $(-\infty, \infty)$ Range: $[0, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow \infty$ $x \rightarrow \infty, y \rightarrow \infty$		$y = \sqrt{x}$ Radical, Neither Domain: $[0, \infty)$ Range: $[0, \infty)$ End Behavior: $x \rightarrow \infty, y \rightarrow \infty$	
$y = x^3$ Cubic, Odd Domain: $(-\infty, \infty)$ Range: $(-\infty, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow -\infty$ $x \rightarrow \infty, y \rightarrow \infty$		$y = \sqrt[3]{x}$ Cube Root, Odd Domain: $(-\infty, \infty)$ Range: $(-\infty, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow -\infty$ $x \rightarrow \infty, y \rightarrow \infty$	
$y = b^x, b > 1$ Exponential, Neither Domain: $(-\infty, \infty)$ Range: $(0, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow 0$ $x \rightarrow \infty, y \rightarrow \infty$		$y = \log_b(x), b > 1$ Log, Neither Domain: $(0, \infty)$ Range: $(-\infty, \infty)$ End Behavior: $x \rightarrow 0^+, y \rightarrow -\infty$ $x \rightarrow \infty, y \rightarrow \infty$	
$y = \frac{1}{x}$ Rational (Inverse), Odd Domain: $(-\infty, 0) \cup (0, \infty)$ Range: $(-\infty, 0) \cup (0, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow 0$ $x \rightarrow \infty, y \rightarrow 0$		$y = \frac{1}{x^2}$ Rational (Inverse Squared), Even Domain: $(-\infty, 0) \cup (0, \infty)$ Range: $(0, \infty)$ End Behavior: $x \rightarrow -\infty, y \rightarrow 0$ $x \rightarrow \infty, y \rightarrow 0$	
$y = \text{int}(x) = [x]$ Greatest Integer, Neither Domain: $(-\infty, \infty)$ Range: $\{y : y \in \mathbb{Z}\}$ (integers) End Behavior: $x \rightarrow -\infty, y \rightarrow -\infty$ $x \rightarrow \infty, y \rightarrow \infty$		$y = C$ ($y = 2$ in the graph) Constant, Even Domain: $(-\infty, \infty)$ Range: $\{y : y = C\}$ End Behavior: $x \rightarrow -\infty, y \rightarrow C$ $x \rightarrow \infty, y \rightarrow C$	

Conic Sections

Conic: Equation:	Circle Center: (h, k)	Parabola Vertex: (h, k)	Ellipse Center: (h, k) a always larger than b	Hyperbola Center: (h, k) a always before the “-”
Equation (Horizontal)	$(x-h)^2 + (y-k)^2 = r^2$	$x = a(y-k)^2 + h$ or $x-h = a(y-k)^2$ or $b(x-h) = (y-k)^2$	$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$	$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$ Asymptotes: $y-k = \pm \frac{b}{a}(x-h)$
Graph (Horizontal)		(Positive Coefficient) 		
Equation (Vertical)	Same	$y = a(x-h)^2 + k$ or $y-k = a(x-h)^2$ or $b(y-k) = (x-h)^2$	$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$	$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$ Asymptotes: $y-k = \pm \frac{a}{b}(x-h)$
Graph (Vertical)	Same	(Positive Coefficient) 		
Additional Information	To get r : $y = \pm \sqrt{r^2 - (x-h)^2} + k$	For $x-h = a(y-k)^2$: $p = \frac{1}{4a}; a = \frac{1}{4p}$ For $b(x-h) = (y-k)^2$: $b = 4p; p = \frac{b}{4}$ $p = \text{focal length}$ Negative Coefficients: Flip parabola	$c^2 = a^2 - b^2$	$c^2 = a^2 + b^2$