

8-8 Linear and Quadratic Functions

Objective: To graph linear and quadratic functions.

Vocabulary

Graph of a function The graph of an equation that defines a function.

Linear function A function defined by $f(x) = mx + b$. For example,
 $f(x) = 2x + 3$.

Quadratic function A function defined by $f(x) = ax^2 + bx + c$ ($a \neq 0$).
 For example, $f(x) = 2x^2 - x - 1$.

Parabola The graph of $f(x) = ax^2 + bx + c$, where the domain of f is the set of real numbers and $a \neq 0$. If $a > 0$, the parabola opens upward; if $a < 0$, the parabola opens downward.

Maximum point of a parabola The highest point on a parabola that opens downward; the point whose y -coordinate is the *greatest value* of the corresponding function.

Minimum point of a parabola The lowest point on a parabola that opens upward; the point whose y -coordinate is the *least value* of the corresponding function.

Axis of symmetry of a parabola The vertical line containing the maximum or minimum point of the parabola. The axis of symmetry of

$$y = ax^2 + bx + c \quad (a \neq 0) \text{ is } x = -\frac{b}{2a}.$$

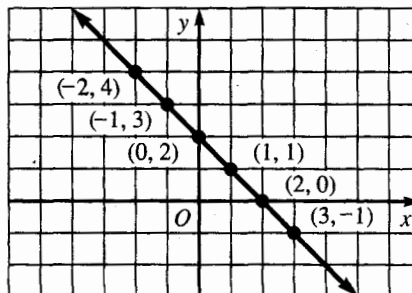
Vertex of a parabola The maximum or minimum point of the parabola. The

$$x\text{-coordinate of the vertex of } y = ax^2 + bx + c \quad (a \neq 0) \text{ is } x = -\frac{b}{2a}.$$

Example 1 Graph the function h defined by the equation $y = h(x) = -x + 2$.

Solution Find the coordinates of selected points as shown in the table below. Plot the points and connect them with a line.

x	$-x + 2 = y$
-2	$-(-2) + 2 = 4$
-1	$-(-1) + 2 = 3$
0	$-(0) + 2 = 2$
1	$-(1) + 2 = 1$
2	$-(2) + 2 = 0$
3	$-(3) + 2 = -1$



Draw the graph of each linear function. You may wish to verify your graphs on a computer or a graphing calculator.

1. $g: x \rightarrow x - 2$

2. $f: x \rightarrow -x + 3$

3. $g(x) = 2 - \frac{1}{2}x$

4. $d(x) = -\frac{2}{3}x$

5. $h(x) = -4$

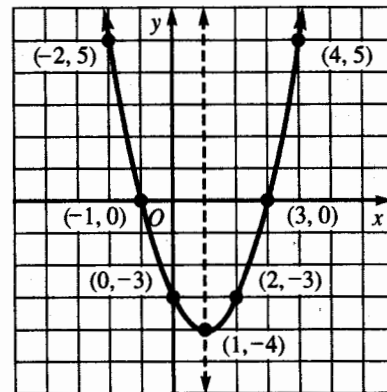
6. $n(x) = 5$

8-8 Linear and Quadratic Functions (continued)

Example 2 Find the coordinates of the vertex of the function $g(x) = x^2 - 2x - 3$. Then give the equation of the axis of symmetry. Use the vertex and four other points to graph the equation.

- Solution**
- x -coordinate of vertex $= -\frac{b}{2a} = -\frac{-2}{2} = 1$
 - To find the y -coordinate of the vertex, substitute 1 for x .
 $y = x^2 - 2x - 3 = (1)^2 - 2(1) - 3 = 1 - 2 - 3 = -4$
 The vertex is $(1, -4)$.
 - The axis of symmetry is the line $x = 1$.
 - For values of x , select three numbers greater than 1 and three numbers less than 1 to obtain paired points with the same y -coordinate.

x	$x^2 - 2x - 3 = y$
-2	$(-2)^2 - 2(-2) - 3 = 5$
-1	$(-1)^2 - 2(-1) - 3 = 0$
0	$(0)^2 - 2(0) - 3 = -3$
1	$(1)^2 - 2(1) - 3 = -4$
2	$(2)^2 - 2(2) - 3 = -3$
3	$(3)^2 - 2(3) - 3 = 0$
4	$(4)^2 - 2(4) - 3 = 5$



- Plot the points. Connect them with a smooth curve.

Find the vertex and the axis of symmetry of the graph of each equation. Use the vertex and at least four other points to graph the equation.

7. $y = 2 - x^2$

8. $y = -2x^2$

9. $y = x^2 - 3x$

10. $y = -x^2 + x$

11. $y = -x^2 - x + 2$

12. $y = x^2 + 2x - 3$

Mixed Review Exercises

Find the range of each function.

1. $f(x) = 2x^2 + 3, D = \{0, 1, 2\}$

2. $m(b) = b^3 + 4, D = \{-1, 1, 2\}$

Translate each phrase into a variable expression.

3. 3 times the sum of a number and 2

4. The difference between a number and 6

5. The product of a number and 7

6. 4 less than one half of a number